

## FAULT ANALYSIS: AN APPLICATION OF THE THEVENIN'S METHOD TO 330kV TRANSMISSION GRID SYSTEM IN NIGERIA

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### ABSTRACT

*Thevenin's method of approach for analyzing electrical power circuit parameters is presented in this paper. Two different MATLAB programs were written to determine the performance of the Nigerian National Electric Power Authority [NEPA] 330kV transmission grid system. One of the MATLAB programs was for Load flow study to know the pre-fault condition which is based on Gauss-Seidel method; while the other is for Short Circuit Studies which indeed made use of Thevenin's Method of approach to solve problems on a closed circuit. Various kinds of Line-Line faults and Line-Ground faults were simulated and was found that the energy released from a 3-phase fault is most enormous.*

### INTRODUCTION

The purpose of an electrical power system is to generate and supply electrical energy to consumers with reliability and economy. Reliability is very significant in system design, but should not be pursued as an end in itself without taking cost factors into consideration (the cost, especially to repair or re-construct a damaged system as a result of fault).

Security of supply, therefore, can be better by improving plant design, increasing the spare capacity margin and arranging alternative circuits to supply loads. Sub-division of the system into zones, each controlled by switchgear in association with protective gear, provides flexibility during normal operation and ensures a minimum of dislocation following a breakdown.

The greatest threat to the security of a supply system is the short circuit, which imposes a sudden and sometimes violent change on system operation. The large current which flows, accompanied by the localized release of a considerable quantity of energy can cause fire at the fault location and mechanical damage throughout the system, particularly to machine and transformer windings. Rapid isolation of the fault by the nearest switchgear will minimize the damage and disruption caused to the system.

The risk of fault occurring in a Grid System, however slight for each, is multiplied by the number of such items which are closely associated in an extensive system as any fault produces repercussions throughout the network. When the system is so large like this, the chance of a fault occurring and the disturbance it will bring are both so enormous that without equipment to remove faults, the system will become inoperable.

The objective of the system will be defeated if adequate provision for fault clearance is not made. The installation of switchgear alone is insufficient, discriminative protective gear, designed according to the characteristics and requirements of the power system must be provided to control the switchgear.

A system is not properly designed and managed if it is not adequately protected. This is the measure of the importance of protective system in modern practice and of the responsibility vested in the protective engineer.

Fault analysis can be broadly grouped into symmetrical and unsymmetrical faults. The causes of faults are numerous, e.g. lightning, heavy winds, trees falling across lines, vehicles colliding with towers or poles, e.t.c. A fault involving all the three phases is known as symmetrical fault, while one involving only one or two phases is known as unsymmetrical faults. Single line to ground, line to line and two lines to ground faults are unsymmetrical faults. Majority of the faults are unsymmetrical. However, the circuit breaker rated MVA breaking capacity is based on 3phase fault MVA. A 3-phase fault inflicts greatest damage to the power system, except in a situation where a single line to ground fault is very close to a solidly grounded generator's terminal. In this instance the severity of single line to ground fault is greater than that of 3phase balance fault.

Short circuit studies involve finding the voltages and currents distribution throughout the system during fault conditions so that the protective devices may be set to detect the fault and isolate the faulty portion of the system so as to minimize the harmful effects of such contingencies.

The current trend of erratic power supply and system collapse in Nigeria has made this



project study a paramount importance to the nation's power industry.

**EQUATION OF MACHINES**  
**Synchronous Generators**

Though the analysis of short circuit on a loaded synchronous machine is complicated, we cannot run away from the complication because a short circuit can occur at any time not minding loaded or unloaded condition.

Since this study involves the Grid of very large interconnected system, the synchronous machines (generators) will be replaced by their corresponding circuit models having voltage behind sub-transient reactance in series with sub-transient reactance while the remaining passive network components remain unchanged.

The circuit model of this representation is illustrated in Fig. 2(a), while its phasor representation is given in Fig. 2(b). The equation for the induced e.m.f [I.J. Nagrath and D.P. Kothari, 1998], is given as:

$$E_g'' = V^0 + jI^0 X_d'' \tag{1a}$$

$$E_g'' = I^0 r_a + jI^0 X_d'' \tag{1b}$$

where;

$E_g''$  = Voltage behind the sub-transient reactance.

$V^0$  = terminal voltage.

$I^0$  = machine loaded current.

$r_a$  = armature resistance.

$X_d''$  = Sub-transient reactance.

**Power System Equation**

**Load Representation**

During sub-transient period, power system loads, other than motors are represented by the equivalent circuit as static impedance or admittance to ground.

For the purpose of short circuit analysis in order to select appropriate circuit breaker to clear a fault instantly before transient condition on a power system, pre-fault condition of the system (i.e. pre-fault voltages and currents) should be known. This can be obtained from the load flow solution for the power system; the initial value of the current for a constant current representation is obtained from:

$$I_{po} = \frac{P_{lp} - jQ_{lp}}{V_p^*} \tag{2}$$

where;

$P_{lp}$  and  $Q_{lp}$  = the scheduled bus load.

$V_p^*$  = the calculated voltage.

The current  $I_{po}$  flows from bus P to ground, that is, to bus 0.

The magnitude and power factor angle of  $I_{po}$  remain constant.

The static admittance;

$$y_{po} = I_{po} \tag{3}$$

where;

$V_p^*$  = the calculated bus voltage and

$V_o$  (the ground voltage) = 0.

Therefore,

$$y_{po} = \frac{I_{po}}{V_p^*} \tag{4}$$

**Network Performance Equation**

The Gauss-Seidel method of solution used for the load flow equation can be applied to describe the performance of a network during a sub-transient period, using the bus admittance matrix with ground as reference. The voltage equation for bus P [as reported by Elgerd, O.I., 1973] is given by:

$$V_p = \frac{(P_p - jQ_p)L_p}{V_p^*} - \sum_{q=1}^{p-1} Y_{pq} V_q^{k+1} - \sum_{q=p+1}^n Y_{pq} V_q^k \tag{5}$$

where;

$$Y_{pq} = Y_{pq} L_p; L_p = \frac{1}{Y_{pp}}$$

The term  $\frac{(P_p - jQ_p)}{V_p^*}$  in equation 5

represents the load current at bus P. For the constant load current representation,

$$\frac{P_p - jQ_p}{(V_p^k)^*} = |I_{po}| \angle (\Theta_p^k + \Phi_p) \tag{6}$$

where;

$\Phi_p$  = the power factor angle,

and  $\Theta_p^k$  = the angle of voltage with respect to the reference.

When the constant power is used to represent the load,  $(P_p - jQ_p)L_p$  will be constant but the bus voltage  $V_p$  will change in any iteration. When the load at bus P is represented by a static admittance to ground, the impressed current at the bus is zero and therefore,

$$\frac{(P_p - jQ_p)L_p}{V_p^*} = 0 \tag{7}$$

For a sub-transient analysis in short circuit studies, the parameters of equation (5) must be modified to include the effect of the equivalent element



required to represent synchronous induction and loads. The line parameters  $Y_{L_{pq}}$  must be modified for the new elements and additional line parameter must be calculated for each new network element.

**METHOD OF SOLUTION**

**Preliminary Calculations**

It had been mentioned earlier that for short circuit studies, it is necessary to have the knowledge of pre-fault voltages and currents. These pre-fault conditions can be obtained from the result of load flow solution by Gauss-Seidel iteration method using  $Y_{BUS}$ , the flowchart of which is illustrated in Fig.5.

The pre-fault machine currents are calculated from load flow by Gauss-Seidel iterative method from:

$$I_{ki} = \frac{P_{ki} - jQ_{ki}}{V_{ki}^*} ; i = 1, 2, \dots, m. \quad 8$$

where;

$P_{ki}$  and  $Q_{ki}$  = the scheduled or calculated machine real and reactive terminal powers.

$V_{ki}^*$  = the last iteration voltage.

$m$  = the number of machines in the system.

The network is then modified to correspond to the desired representation for short circuit studies. Being a linear network of several voltage sources, further calculation can be computed by application of Thevenin's theorem.

**Thevenin's Theorem**

This is a powerful method of solution for a large network. The model representation of the Thevenin's equivalent of the system is shown in Fig. 3(a). The circuit in Fig.3 (a) can be replaced by the one in Fig.3(b) if a ground fault is assumed through  $Z^f$ . Therefore, fault current can be immediately written as:

$$I^f = \frac{V^0}{jX_{TH}'' + Z^f} \quad 9$$

This is a very fast method for computing short circuit fault current.

**Consideration of Pre-Fault Load Current**

If the magnitude of fault current is small, the pre-fault current can be superimposed on the fault current in order to know its effect. But in this instance, it is not necessary because the resulted fault current is satisfactorily large enough (i.e. larger than the specified 10 –20 p.u changes caused in current by short circuit).

Moreover, the load currents and fault current are nearly in quadrant and their phasor sum

is nearly equal to the larger component, which is the fault current. Again, a fault can occur at any time and there is no way of predicting the loading condition of the system at the instant of fault.

**EQUATION FOR SHORT CIRCUIT STUDIES**

It has to be reiterated once again before proceeding on short circuit computation that the admittance bus matrix formed and used in load flow has to be inverted to obtain the impedance bus matrix for easy computation. Building the  $Z_{BUS}$  algorithm is of paramount importance in the calculation process. The best method employed for digital calculation is a step-by-step programmable technique, which proceeds branch by branch. It has the advantage that any modification of the network does not require complete rebuilding of  $Z_{BUS}$ . It is described in terms of modifying an existing bus impedance matrix designated as  $|Z_{bus}|_{old}$ . The new modified matrix is designated as  $|Z_{bus}|_{new}$ . This is described as follows:

$Z_b$  = branch impedance

$$Z_{Bus(Old)} \longrightarrow Z_{Bus(new)}$$

In the process of adding a new bus to an old one, the likely modifications are:

- (i) Addition of Tree Branch  $Z_b$  from a New Bus k to Reference.
- (ii) Addition of Tree Branch  $Z_b$  from a New Bus k to Old Bus j.
- (iii) Addition of a Link  $Z_b$  between an Old Bus j and Reference.
- (iv) Addition of Link  $Z_b$  between two Old Busses i and j.
- (v) Modification of  $[Z_{bus}]$  for changes in Network.

The effect of (i) above is that  $Z_{BUS}$  dimension goes up by one, (ii) above will form a new loop without affecting the  $Z_{BUS}$  dimension. For (iii), (iv) and (v), the  $Z_{BUS}$  remains unaffected at all. To know more about this technique, read more about the effect. [B.R. Gupta, 1993] and [Nagrath and Kothari, 1998].

**Calculation of Line Current**

As mentioned earlier, the aim of a short circuit study is to determine fault current, bus voltages and line currents under fault conditions. The line currents can be calculated from the values of bus voltages determined in section 2.4.3. From Fig. 4, the current in the line joining ith and kth buses is given by:

$$I_{ik}^n = \frac{V_i^n - V_k^n}{Z_b^n} \quad 10$$



where:

$n$  = the sequence,  $n = 0,1,2$ .

$I_{ik}^n$  =  $n$ th sequence current from  $i$ th bus to  $k$ th bus.

$V_i^n$  =  $n$ th sequence voltage at  $i$ th bus.

$V_k^n$  =  $n$ th sequence voltage at  $k$ th bus.

$Z_b^n$  =  $n$ th sequence impedance of branch connecting  $i$ th and  $k$ th buses.

**Sequence Component for Short Circuit Studies**

Due to the effect of large changes (between 10 –20 p.u) brought about by short circuit fault, a pre-fault load current is very negligible compared to the fault current. It can be assumed that all pre-fault bus voltages are 1p.u; [B.R. Gupta, 1993]. Therefore, the sequence quantities can be represented as follows:

$$V_{0-bus} = -|Z_{0-bus}| I_{0-bus} \tag{11a}$$

$$V_{1-bus} = E_{bus} - |Z_{1-bus}| I_{1-bus} \tag{11b}$$

$$V_{2-bus} = -|Z_{2-bus}| I_{2-bus} \tag{11c}$$

where;

$V_{0-bus}$  = zero sequence bus voltage vector ( $n \times 1$ ), general entry  $V_k^0$ .

$V_{1-bus}$  = positive sequence bus voltage vector ( $n \times 1$ ), general entry  $V_k^1$ .

$V_{2-bus}$  = negative sequence voltage vector ( $n \times 1$ ), general entry  $V_k^2$ .

$I_{0-bus}$  = zero sequence bus current vector ( $n \times 1$ ), general entry  $I_k^0$ .

$I_{1-bus}$  = positive sequence bus current vector ( $n \times 1$ ), general entry  $I_k^1$ .

$I_{2-bus}$  = negative sequence bus current vector ( $n \times 1$ ), general entry  $I_k^2$ .

$|Z_{0-bus}|$  = zero sequence bus impedance matrix ( $n \times n$ ), general entry  $Z_{ik}^0$ .

$|Z_{1-bus}|$  = positive sequence bus impedance matrix ( $n \times n$ ), general entry  $Z_{ik}^1$ .

$|Z_{2-bus}|$  = negative sequence bus impedance matrix ( $n \times n$ ), general entry  $Z_{ik}^2$ .

Where superscripts on each of the symbols  $V_k^0, I_k^1$  and  $Z_{ik}^2$  indicates the sequence while the subscripts indicates bus number.

**Symmetrical and Unsymmetrical Fault Equations**

The equation for fault analysis can be developed using Equations (11) with the assumption that network is terminated at the faulted bus (bus  $k$ ).

**Three-Phase Fault**

The negative sequence and zero sequence quantities are absent in a three-phase fault (because both of them are equal to zero). Also all currents except the current at the faulted bus ( $I_k^1$ ) are zero.

Hence we have:

$$V_k^1 = E - Z_{kk}^1 I_k^1 \tag{12}$$

If  $Z_f$  is the fault impedance, then;

$$I_k^1 = \frac{E}{Z_{kk}^1 + Z_f} \tag{13}$$

The effect of the fault on other busses linked to the faulted bus can be obtained as:

$$V_i^1 = E - Z_{ik}^1 I_k^1 = E \left[ 1 - \frac{Z_{ik}^1}{Z_{kk}^1 + Z_f} \right] \tag{14}$$

(For  $i = 1, 2, \dots, n$ ).

The summary of the flowchart for 3-phase fault is shown on Fig.6.

**Single Line-To-Ground Fault**

For a single line to earth fault, all sequence currents of other buses other than faulted bus are zero. Also the sequence currents on the faulted bus are equal and the sum of the sequence voltages is given as:

$$V_k^0 + V_k^1 + V_k^2 = 3Z_f I_k^1 \tag{15}$$

Combining the above explanation with equations (2.11) and (2.15) we have:

$$I_k^1 = \frac{E}{Z_{kk}^0 + Z_{kk}^1 + Z_{kk}^2 + 3Z_f} \tag{16}$$

The sequence voltages at all other busses linked to the faulted bus can be given as:

$$V_i^0 = -Z_{ik}^0 I_k^0 = Z_{ik}^0 I_k^1 = \frac{-Z_{ik}^0 E}{Z_{kk}^0 + Z_{kk}^1 + Z_{kk}^2 + 3Z_f} \tag{17a}$$

$$V_i^1 = E - Z_{ik}^1 I_k^1 = E \left[ \frac{Z_{kk}^0 + Z_{kk}^1 + Z_{kk}^2 + 3Z_f - Z_{ik}^1}{Z_{kk}^0 + Z_{kk}^1 + Z_{kk}^2 + 3Z_f} \right] \tag{17b}$$

$$V_i^2 = -Z_{ik}^2 I_k^2 = -Z_{ik}^2 I_k^1 = \frac{-Z_{ik}^2 E}{Z_{kk}^0 + Z_{kk}^1 + Z_{kk}^2 + 3Z_f} \tag{17c}$$



(For  $i = 1, 2, \dots, n$ ).

The summary of the flowchart for single line-to-ground fault is shown on Fig.7.

**Line-To-Line Fault**

For a line – to – line fault, all sequence currents at busses other than the faulted bus are zero. Also, on the faulted bus, the zero sequence quantities are zero. Therefore,

$$V_k^1 = V_k^2 + I_k^1 Z_f \tag{18}$$

After few manipulations we have:

$$I_k^1 = \frac{E}{Z_{kk}^1 + Z_{kk}^2 + Z_f} \tag{19}$$

The positive and negative sequence voltages at busses linked to the faulted bus are given as:

$$V_i^1 = E - Z_{ik}^1 I_k^1 = E \left[ \frac{Z_{kk}^1 + Z_{kk}^2 + Z_f - Z_{ik}^1}{Z_{kk}^1 + Z_{kk}^2 + Z_f} \right] \tag{20a}$$

$$V_i^2 = -Z_{ik}^2 I_k^2 = Z_{ik}^2 I_k^1 = \frac{Z_{ik}^2 E}{Z_{kk}^1 + Z_{kk}^2 + Z_f} \tag{20b}$$

The summary of the flowchart for Line – To – Line Fault is shown on Fig.8.

**Double Line-To-Ground Fault**

For a double line – to – ground fault, all sequence currents at busses other than the faulted bus are zero. Also the sum of the sequence currents on the faulted bus is equal to zero.

Moreover, positive sequence voltage and negative sequence voltage at the faulted bus are equal and lastly,

$$V_k^0 - V_k^1 = 3I_k^0 Z_f \tag{21}$$

Combining all the above explanations with equations (2.11) and (2.21), we have:

$$I_k^1 = \frac{E - V_k^1}{Z_{kk}^1} \tag{22a}$$

$$I_k^2 = -\frac{V_k^2}{Z_{kk}^2} = -\frac{V_k^1}{Z_{kk}^2} \tag{22b}$$

$$I_k^0 = \frac{V_k^0}{Z_{kk}^0} = -\frac{V_k^1}{Z_{kk}^0 + 3Z_f} \tag{22c}$$

As a result of the validity of the above explanations and equations, we have:

$$V_k^1 = V_k^2 = \frac{E \left( Z_{kk}^0 + 3Z_f \right) Z_{kk}^2}{Z_{kk}^1 \left( Z_{kk}^2 + Z_{kk}^0 + 3Z_f \right) + Z_{kk}^2 \left( Z_{kk}^0 + 3Z_f \right)} \tag{23}$$

Let

$$Z_{kk}^1 \left( Z_{kk}^2 + Z_{kk}^0 + 3Z_f \right) + Z_{kk}^2 \left( Z_{kk}^0 + 3Z_f \right) = \Delta \tag{24}$$

Hence,

$$I_k^1 = \left( Z_{kk}^2 + Z_{kk}^0 + 3Z_f \right) E / \Delta \tag{24a}$$

$$I_k^2 = -E \left( Z_{kk}^0 + 3Z_f \right) / \Delta \tag{24b}$$

$$I_k^0 = -EZ_{kk}^2 / \Delta \tag{24c}$$

The sequence voltages at the buses linked to the faulted bus are given as:

$$V_i^0 = -Z_{ik}^0 I_k^0 = EZ_{ik}^0 Z_{kk}^2 / \Delta \tag{25a}$$

$$V_i^1 = E - Z_{ik}^1 I_k^1 = E \left[ \Delta - Z_{ik}^1 \left( Z_{kk}^2 Z_{kk}^0 + 3Z_f \right) \right] / \Delta \tag{25b}$$

$$V_i^2 = -Z_{ik}^2 I_k^2 = Z_{ik}^2 \left[ Z_{kk}^0 + 3Z_f \right] E / \Delta \tag{25c}$$

(for  $i = 1, 2, \dots, n$ ).

The summary of the flowchart for Double Line – To – Ground fault is shown on Fig.9.

**COMPARISON OF SINGLE LINE-TO-GROUND FAULT AND 3-PHASE FAULT CURRENTS**

This comparison is necessary because of the earlier statement in this research study that single line – to – ground fault is more severe than that of 3 – phase fault if the fault is located very close to the terminal of a solidly grounded generator.

The fault impedance can be assumed to be zero because of the enormous effect of the fault current. In addition, if the impedances  $Z_1, Z_2$  and  $Z_0$  are assumed to be pure reactances ( $X_1, X_2$  and  $X_0$ ), then, for a 3 – phase fault,

$$I_a = \frac{E}{jX_1} \tag{26}$$

and that of single line – to – ground fault is given as:

$$I_a = \frac{3E}{jX_1 + jX_2 + jX_0} \tag{27}$$

The three practical possibilities are as follows:

- (i) Fault at the terminals of neutral solidly grounded generator, (for generator  $X_0 \ll X_1$ ), and it is assumed that  $X_1 = X_2$  for sub-transient condition which is the case for the short circuit studies. At

this instance single line – to – ground fault is more severe than a 3 – phase fault.

- (ii) If a generator is grounded through a reactance  $X_n$ , this does not have any effect on a 3 – phase fault current, but a single line – to – ground fault will have a fault current:

$$I_a = \frac{3E}{j(X_1 + X_2 + X_0 + 3X_n)}$$

- (iii)

To this end the relative severity of 3 – phase fault and single line – to – ground fault will depend on the value of  $X_n$ .

For a fault on a transmission line (which is the case study)  $X_0 \gg X_1$  so that for a fault on a line sufficiently far away from the generator terminals, 3 – p phase fault current is more than single line – to – ground fault current.

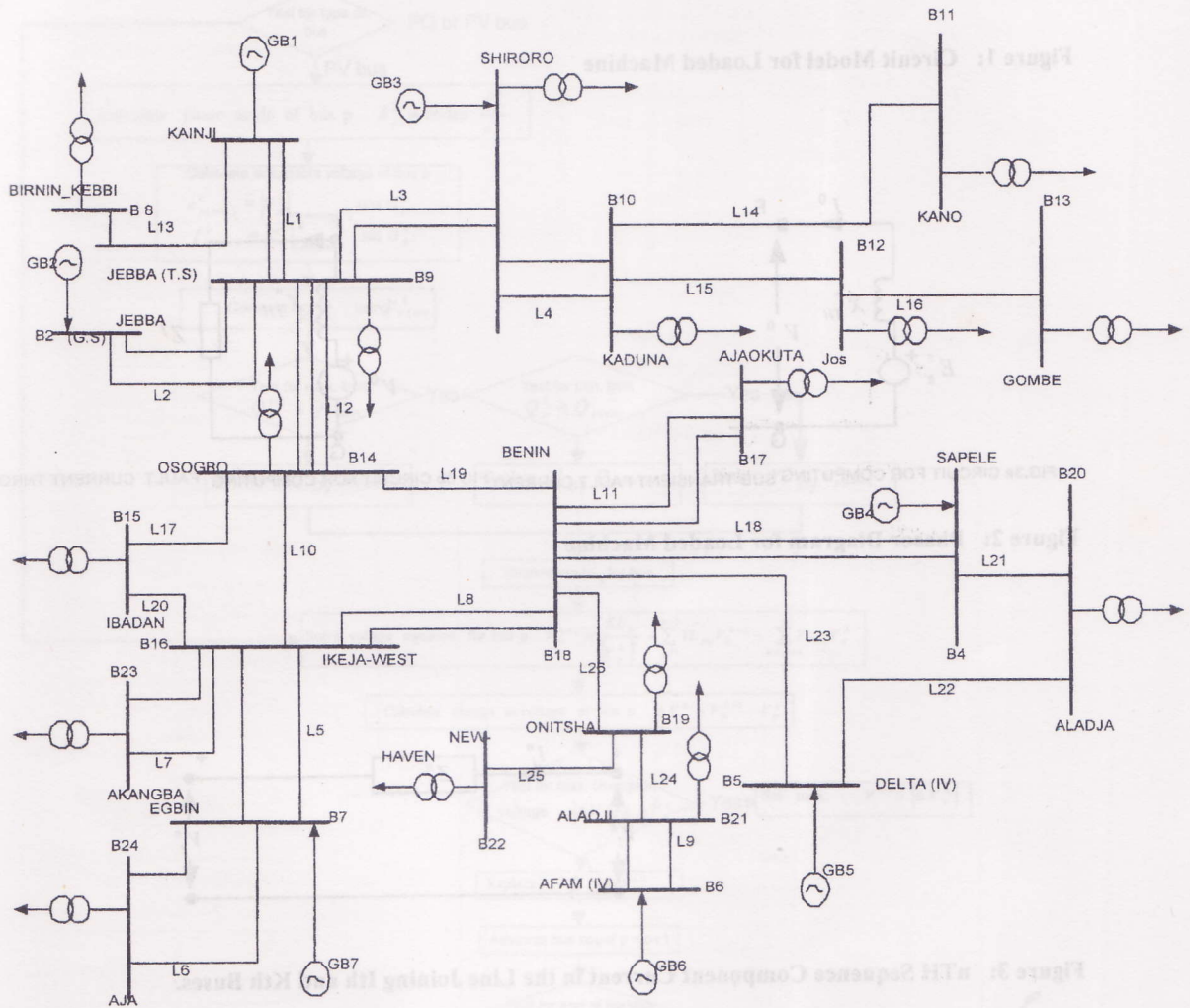


Figure 1: Line Diagram of Existing National 330kv Network.



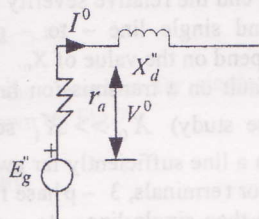


FIG.2a CIRCUIT MODEL FOR LOADED MACHINE.

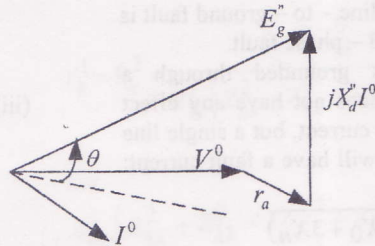


FIG.2b PHASOR DIAGRAM FOR LOADED MACHINE.

Figure 1: Circuit Model for Loaded Machine

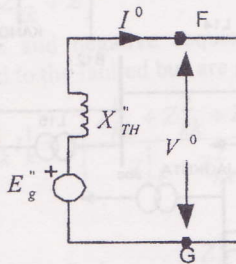


FIG.3a CIRCUIT FOR COMPUTING SUB-TRANSIENT FAULT CURRENT.

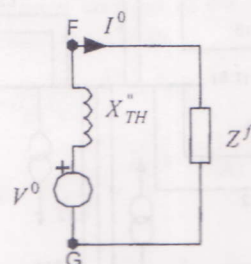


FIG.3b CIRCUIT FOR COMPUTING FAULT CURRENT THROUGH  $Z^f$

Figure 2: Phasor Diagram for Loaded Machine

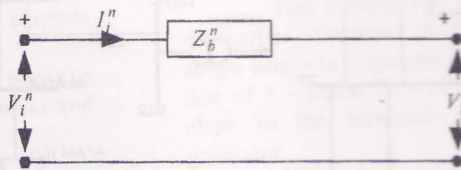


Figure 3: nTH Sequence Component Current in the Line Joining Ith and Kth Buses.

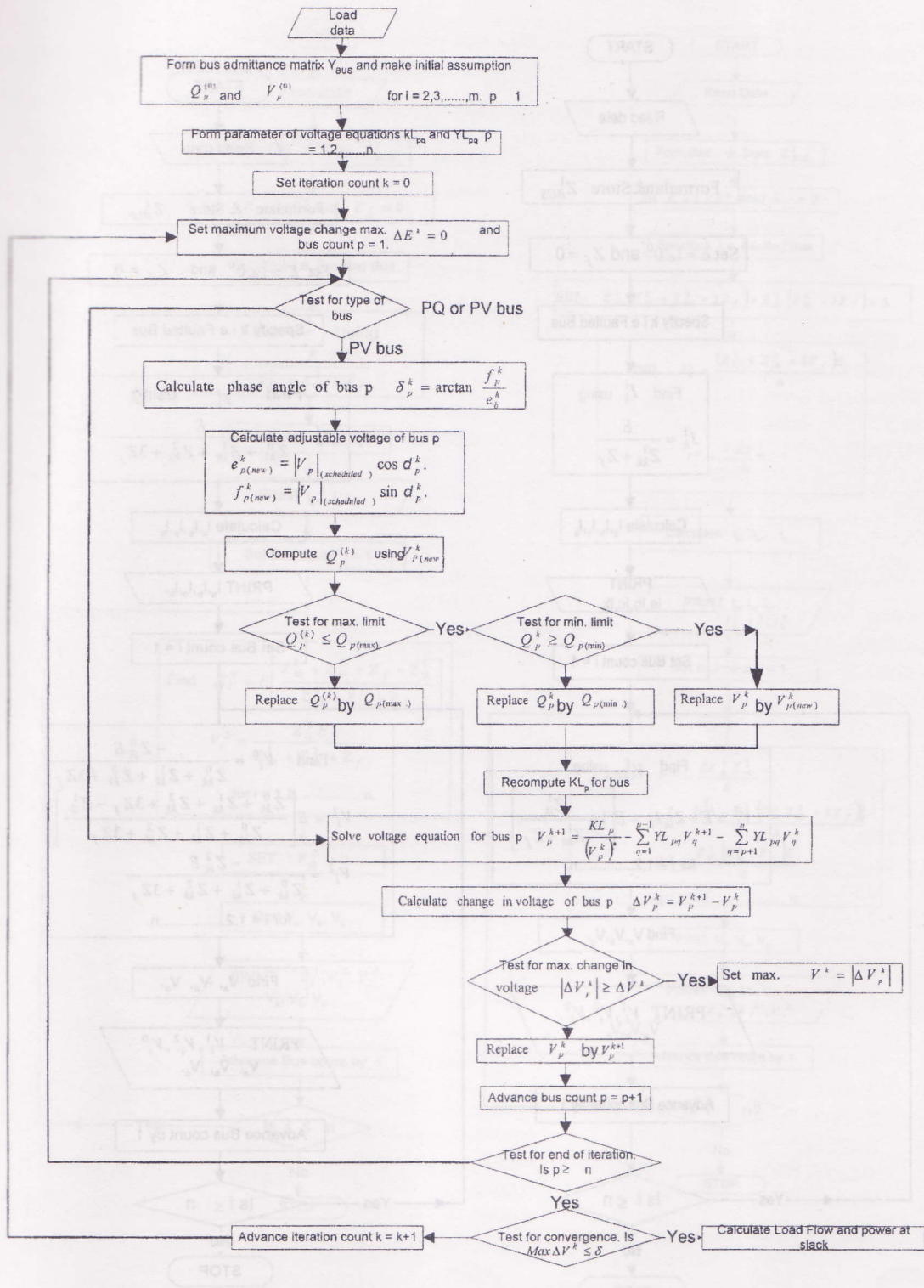


Figure 4: Flow Chart for Load Flow Solution: Gauss-Seidel Iterative Methods.



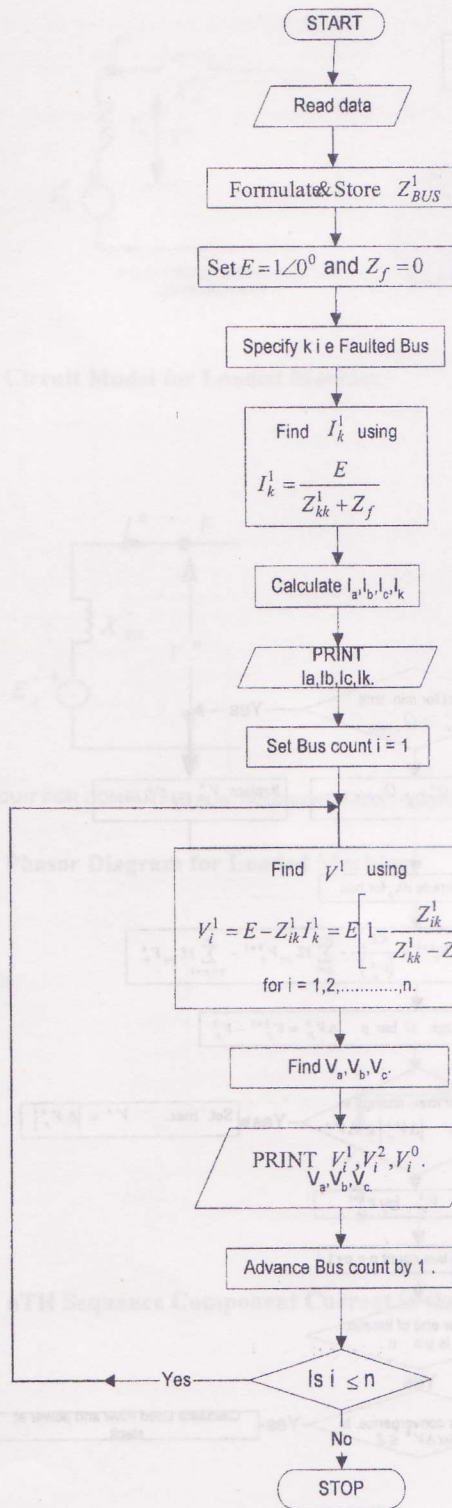


Figure 5: Flow Chart For 3-Phase (Symmetrical) Fault.

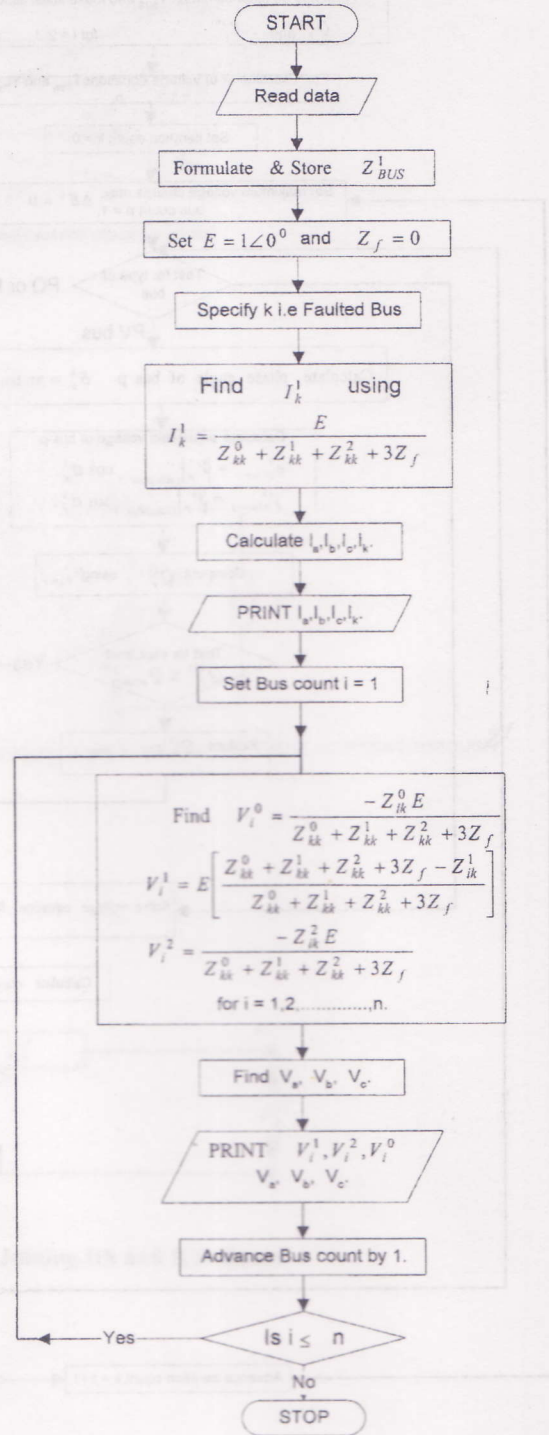


Figure 6: Flow Chart for Single-Line-To-Ground Unsymmetrical Fault.



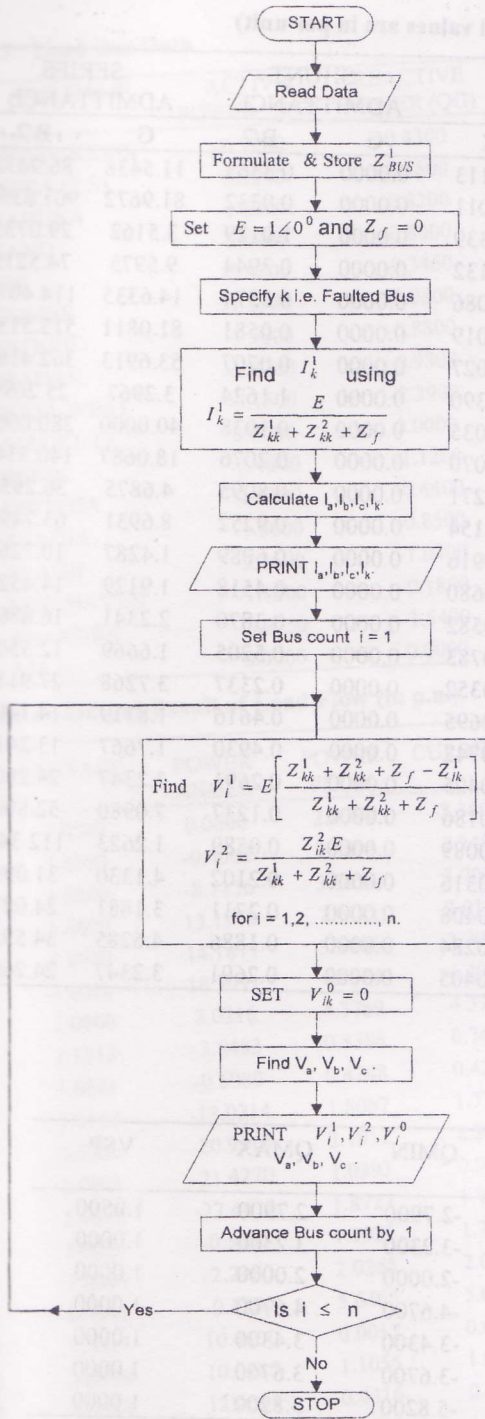


Figure 7: Flow Chart for Line-To-Line Unsymmetrical Fault.

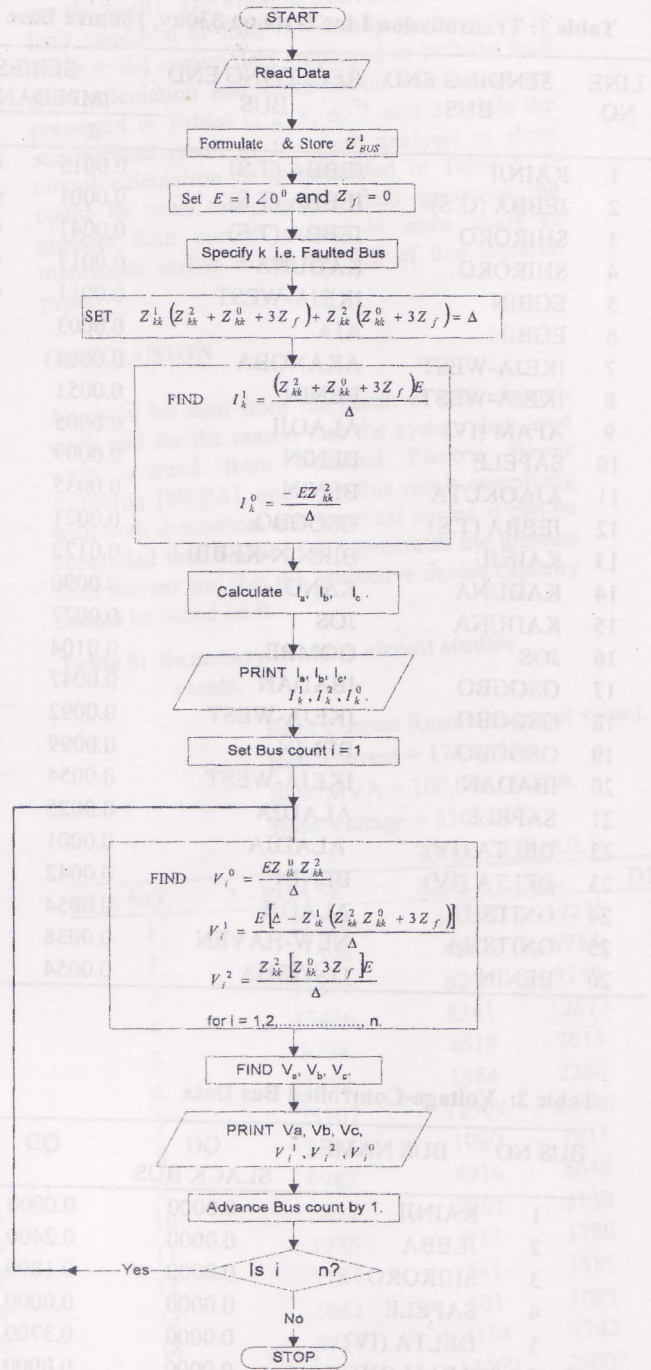


Figure 8: Flow Chart for Double Line-To-Ground Unsymmetrical Fault.



**Table 1: Transmission Line Data on 330kv, 100mva Base (All values are in per unit)**

LINE NO.	SENDING END BUS	RECEIVING END BUS	SERIES IMPEDANCE		SHUNT ADMITTANCE		SERIES ADMITTANCE	
			R	X	G	B/2	G	B/2
1	KAINJI	JEBBA (T.S)	0.0015	0.0113	0.0000	0.3363	11.5438	86.9632
2	JEBBA (G.S)	JEBBA (T.S)	0.0001	0.0011	0.0000	0.0332	81.9672	901.6393
3	SHIRORO	JEBBA (T.S)	0.0041	0.0339	0.0000	1.0129	3.5162	29.0733
4	SHIRORO	KADUNA	0.0017	0.0132	0.0000	0.3944	9.5975	74.5215
5	EGBIN	IKEJA-WEST	0.0011	0.0086	0.0000	0.2574	14.6335	114.4073
6	EGBIN	AJA	0.0003	0.0019	0.0000	0.0581	81.0811	513.5135
7	IKEJA-WEST	AKANGBA	0.0004	0.0027	0.0000	0.0707	53.6913	362.4161
8	IKEJA-WEST	BENIN	0.0051	0.0390	0.0000	1.1624	3.2967	25.2099
9	AFAM (IV)	ALAOJI	0.0005	0.0035	0.0000	0.1038	40.0000	280.0000
10	SAPELE	BENIN	0.0009	0.0070	0.0000	0.2076	18.0687	140.5340
11	AJAKUTA	BENIN	0.0035	0.0271	0.0000	0.8095	4.6875	36.2950
12	JEBBA (T.S)	OSOGBO	0.0021	0.0154	0.0000	0.9252	8.6931	63.7496
13	KAINJI	BIRNIN-KEBBI	0.0122	0.0916	0.0000	0.6089	1.4287	10.7267
14	KADUNA	KANO	0.0090	0.0680	0.0000	0.4518	1.9129	14.4527
15	KADUNA	JOS	0.0077	0.0582	0.0000	0.3870	2.2341	16.8865
16	JOS	GOMBE	0.0104	0.0783	0.0000	0.5205	1.6669	12.5500
17	OSOGBO	IBADAN	0.0047	0.0352	0.0000	0.2337	3.7268	27.9115
18	OSOGBO	IKEJA-WEST	0.0092	0.0695	0.0000	0.4616	1.8719	14.1407
19	OSOGBO	BENIN	0.0099	0.0742	0.0000	0.4930	1.7667	13.2414
20	IBADAN	IKEJA-WEST	0.0054	0.0405	0.0000	0.2691	3.2347	24.2601
21	SAPELE	ALADJA	0.0025	0.0186	0.0000	0.1237	7.0980	52.8094
22	DELTA (IV)	ALADJA	0.0001	0.0089	0.0000	0.0589	1.2623	112.3454
23	DELTA (IV)	BENIN	0.0042	0.0316	0.0000	0.2102	4.1330	31.0962
24	ONITSHA	ALAOJI	0.0054	0.0408	0.0000	0.2711	3.1881	24.0878
25	ONITSHA	NEW-HAVEN	0.0038	0.0284	0.0000	0.1886	4.6285	34.5920
26	BENIN	ONITSHA	0.0054	0.0405	0.0000	0.2691	3.2347	24.2601

**Table 2: Voltage-Controlled Bus Data**

BUS NO.	BUS NAME	QG	QD	QMIN	QMAX	VSP
		SLACK BUS				
1	KAINJI	0.0000	0.0000	-2.7900	2.7900	1.0500
2	JEBBA	0.0000	0.2400	-3.2300	3.2300	1.0000
3	SHIRORO	0.0000	0.1800	-2.0000	2.0000	1.0000
4	SAPELE	0.0000	0.0000	-4.6700	4.6700	1.0000
5	DELTA (IV)	0.0000	0.3700	-3.4300	3.4300	1.0000
6	AFAM (IV)	0.0000	0.0000	-3.6700	3.6700	1.0000
7	EGBIN	0.0000	0.0000	-5.8200	5.8200	1.0000



**Table 3: Load Bus Data**

BUS NO.	BUS NAME	ACTIVE POWER (PG)	REACTIVE POWER (QG)
8	BIRNIN-KEBBI	-0.7200	-0.4300
9	JEBBA (T.S)	-0.3900	-0.1800
10	KADUNA	-1.6100	-0.8200
11	KANO	-2.0400	-0.8000
12	JOS	-0.9800	-0.3460
13	GOMBE	-1.5300	-1.0800
14	OSOGBO	-1.5600	-0.8800
15	IBADAN	-1.8000	-0.9300
16	IKEJA-WEST	-5.1500	-2.2900
17	AJAKUTA	0.0000	0.0000
18	BENIN	-2.4000	-1.1200
19	ONITSHA	-1.0200	-0.4400
20	ALADJA	-1.5600	-0.8500
21	ALAOJI	-2.1600	-1.0400
22	NEW-HAVEN	-1.1000	-0.1800
23	AKANGBA	-3.0750	-1.5400
24	AJA	0.0000	0.0000

**Table 4: Output Result of Load Flow (in p.u.).**

BUS NO	VOLTAGE	POWER ANGLE	POWER FLOW	CURRENT.
1	1.0500	0.0000	2.4783	2.3603
2	1.0000	-0.4063	7.2494	7.2494
3	1.0000	-8.1156	3.7054	3.7054
4	1.0000	13.1979	7.0151	7.0151
5	1.0000	14.1877	3.7006	3.7006
6	1.0000	18.3091	4.4074	4.4074
7	1.0000	2.0216	4.3769	4.3769
8	1.1312	-3.8483	0.8386	0.7413
9	1.0071	-0.6080	0.4248	0.4218
10	1.0167	-13.0214	1.8067	1.7770
11	0.9950	-20.9513	2.1912	2.2022
12	1.0801	-21.4270	1.0393	0.9622
13	1.0670	-27.4478	1.8727	1.7552
14	1.0225	-0.5695	1.7922	1.7528
15	1.0044	-2.2980	2.0265	2.0175
16	0.9911	-0.1259	5.6465	5.6970
17	1.0417	10.4500	0.0017	0.0016
18	1.0189	10.6285	1.1055	1.0850
19	1.0343	12.0094	0.4316	0.4173
20	0.9970	13.3389	1.7721	1.7775
21	1.0002	17.2945	2.3882	2.3878
22	1.0359	10.2950	1.1134	1.0748
23	0.9865	-0.5490	3.4302	3.4773
24	1.0001	2.0226	0.0157	0.0157

**RESULT AND DISCUSSION**

The knowledge of pre-fault voltages and currents is being used in calculating the fault currents for different types of fault condition. (i.e. 3-phase fault, single line-to-ground fault and double line-to-

ground fault). The summarized result of the pre-fault condition or load flow study is presented in Table 4; the system data employed in both the load flow calculation and short circuit calculation are presented in Tables 1, 2, 3, 6, 7, and 8; while the summarized result of the fault analysis or short circuit calculation is as presented in Table 5. It could be seen that 3-phase fault generates the greatest fault current except in some cases as mentioned earlier in section 2.5 of this research paper.

**CONCLUSION**

As could be seen from the result of this research work and for the reason that the system data used were sourced from National Electric Power Authority [NEPA], and with this result complying with both theoretical and practical norms, it can be concluded that 3-phase fault generates the greatest fault current and that the protective device capacity should be based on it.

**Table 5: Summary of short circuit studies result.**

Fault Current Result (in actual value).  
 Base Current = 174.9546A  
 Base MVA = 100,000,000VA.  
 Base Voltage = 330,000V.

BUS NO.	3 - PHASE	TYPE OF FAULT.		
		SLG.	LL.	DLG.
1	22278	11315	19215	19495
2	11598	4201	9784	10127
3	11843	6245	9759	9814
4	15466	8341	12577	12572
5	8738	4619	7613	7653
6	2312	1384	2260	2239
7	25107	12909	21440	21690
8	2152	1080	1911	1934
9	9987	4916	8646	8811
10	5835	2801	5130	5213
11	1935	934	1780	1793
12	1781	841	1585	1607
13	1063	601	1021	1016
14	8954	4154	7742	7907
15	29036	14060	25007	25530
16	21857	9618	18647	19143
17	5729	2864	4961	5052
18	20628	10071	17822	18175
19	3688	1820	3214	3270
20	8808	4258	7697	7830
21	2178	1080	2009	2020
22	2455	1134	2162	2199
23	25452	11945	21795	22307
24	21324	10663	18466	18804



**Table 6: Overhead Lines Parameters**

NO.	OVERHEAD LINE	Z( / KM)	B( / KM)
1	330kV 2 x 350mm <sup>2</sup> (BISON) SINGLE CIRCUIT	0.0428 + j0.3219	3.6074
2	330kV 2 x 350mm <sup>2</sup> (BISON) DOUBLE CIRCUIT	0.0394 + j0.303	3.812

**Table 7: National Grid Machines Parameters.**

Databank of national electric power authority, national control center osogbo.

NO. OF M/C	STATIONS	UNIT	NOM MAX.	NOM	NOM	GEN.	NOM	REACTANCES				PER	UNIT
			APPARENT POWER	ACTIVE POWER	POWER FACTOR	RATING	VOLT. RATING	Rs ohms	Xd	Xq	X'd	X''d	
2	KAINJI HYDRO	5-6	145	120	0.95	126	16	0.0064	0.85	0.55	0.30	0.22	
4	KAINJI HYDRO	7-10	85	80	0.94	85	16		0.76	0.43	0.27	0.18	
2	KAINJI HYDRO	11-12	115	100	0.95	105.26	16	0.0095	0.78	0.44	0.25	0.15	
6	JEBBA HYDRO	1-6	119	96.5	0.85	103.5	16	0.008	0.69	0.48	0.3	0.26	
4	SHIRORO HYDRO	1-4	176.5	150.0055	0.85	176.5	16	0.024PU	0.8	0.49	0.3	0.2	
6	SAPELE STEAM	1-4	136.7	120.573	0.9	133.97	15.75		2.4	1.54	0.215	0.16	
4	SAPELE G.Ts.	1-4	110	75	0.8	110	10.5		2.17	1.92	0.21	0.1333	
6	DELTA (IV) G.Ts.	15-20	133.75	113.6875	0.85	133.8	11.5		1.91	1.835	0.319	0.226	
6	AFAM (IV) G.Ts.	13-18	110	88	0.8	89	10.5		2.17	1.92	0.21	0.154	
6	EGBIN STEAM	1-4	276.9	221.2	0.9	245.8	16	0.004PU	2	2	0.308	0.276	

**Table 8: Generators transformers data ref. System impedance diagrams 1979/80 no. 39761.**

STATION	RATED MVA	XH-L%	XoH-L%	RATIO	TAPPING RANGE
KAINJI 5-6	2 x 145	12	10.8	16/330	1-5 +7.5% - 2.5%
KAINJI 7-10	2 x 184	12	12	16/330	1-4 +7.5% - 3.5%
KAINJI 11-12	2 x 115	12	10.8	16/330	1-5 +7.5% - 2.5%
JEBBA	6 x 119	10.62	10	16/330	1-6 +4.5 - 2.5
SHIRORO 1	200	12.85	*	15.2/330	1-5 +7% - 2.5%
SHIRORO 2	200	13.11	*	15.2/330	1-5 +7% - 2.5%
SHIRORO 3	200	12.9	*	15.2/330	1-5 +7% - 2.5%
SHIRORO 4	200	13.09	*	15.2/330	1-5 +7% - 2.5%
SAPELE G.T	2 x 168.5	13	13	10.5/330	1-4 +5% - 2.5%
SAPELE S.T	6 x 140	14.6	11.6	15.75/330	1-4 +5% - 2.5%
DELTA (IV)	4 x 200	7.84	*	11.5/330	1-5 +5% - 5%
AFAM (IV)	3 x 168.5	13	13	10.5/330	1-4 +5% - 2.5%
EGBIN	6 x 270	10.22	10.22	16/330	1-5 +5% - 5%

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